



Towards Executable Models in Systems Engineering

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Agenda

- **Introduction**
- Models versus Notations
- Mathematical Frameworks
- The S2ML+X Paradigm
- Sigma and WorldLab
- Conclusion

Model-Based Systems Engineering

We entered the era of MBSE but several questions remain to open to a large extent:

- How to make the MBSE process efficient?
- What is a (good) model/modeling language/modeling environment?
- What is the role of **computerized simulation** in MBSE?

These questions are serious and require serious answers.

They are related to **scientific foundations** of MBSE.

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Pragmatic versus Formal Models

“Models” to communicate amongst stakeholders

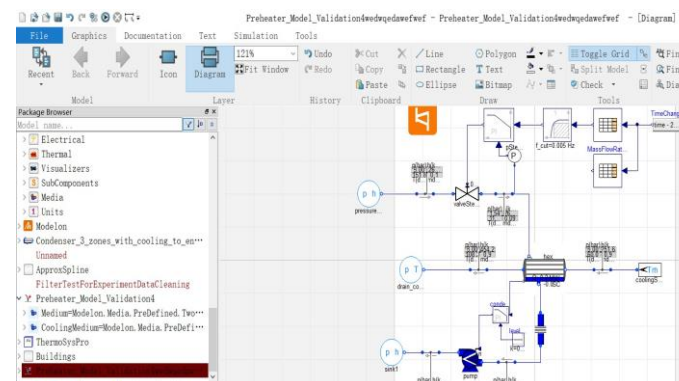


Architectural views	States	Static elements	Dynamic behaviors
Operational analysis			
Functional view			
Constructional view			

Pragmatic “models”

Standardized graphical notations

“Models” to calculate performance indicators



Formal “models”

Differential equations, Automata



Epistemic gap

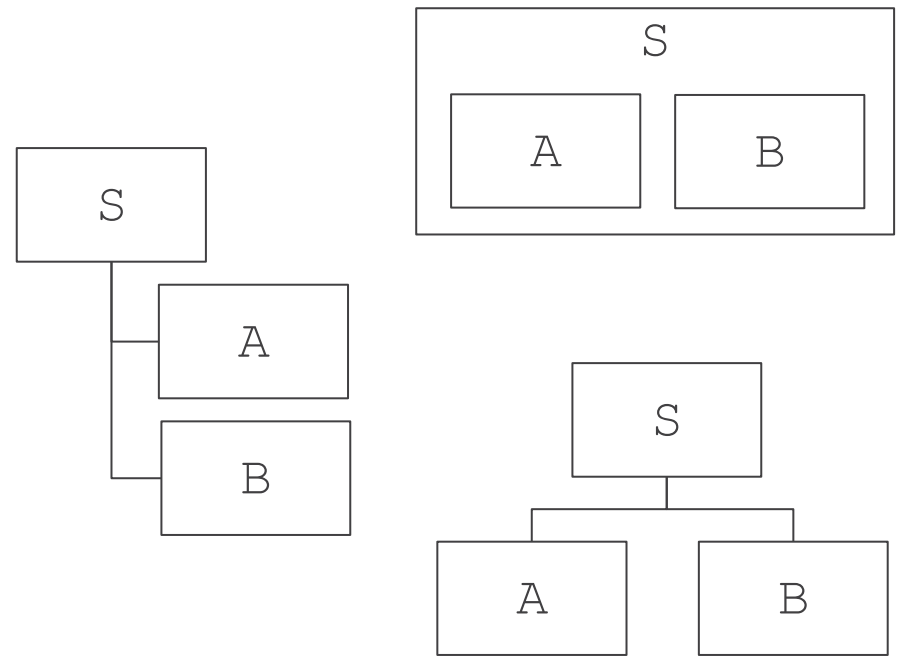
Diagrams Are Not Models

Models are **mathematical objects**

```

block S
  block A
    ...
  end
  block B
    ...
  end
end
  
```

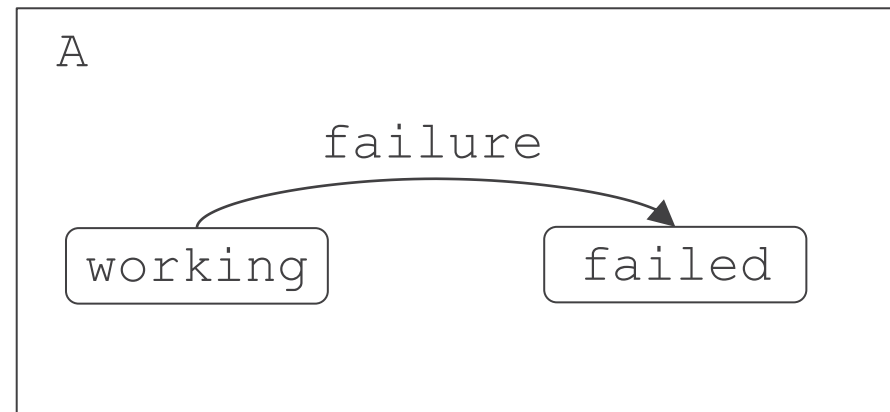
Diagrams are (or more exactly should be) **graphical representations** of models



Formal Models Have a Syntax

```

block A
  state working;
  state failed;
  transition
    failure: working -> failed;
end
  
```



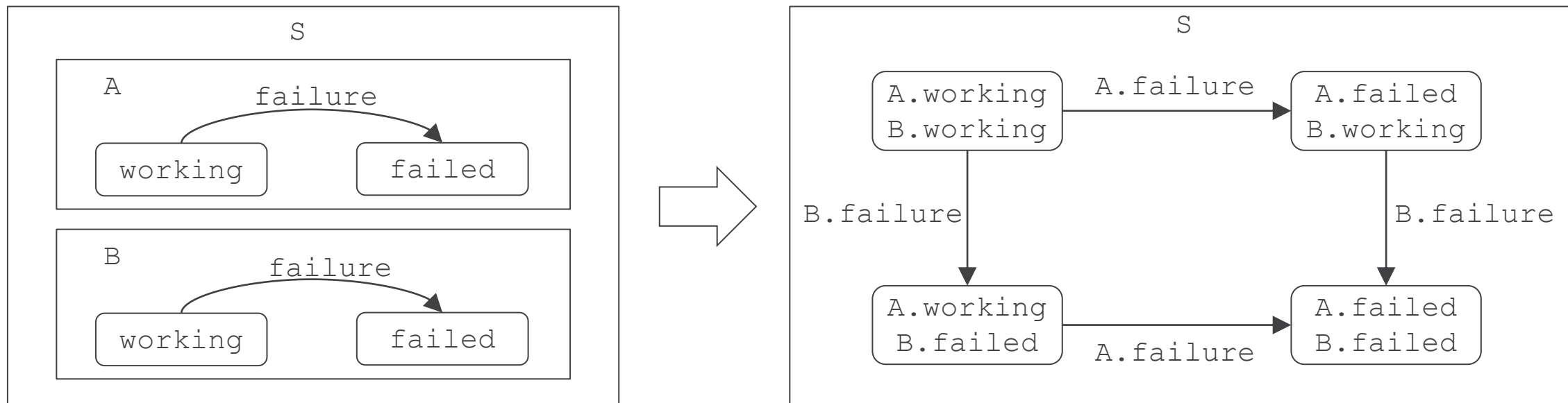
Models are written in **modeling languages**.

There should be a unambiguous means to determine whether a given text (or diagram) is a correct a model or not. This means is called the **syntax** of the models, often described by means of a **grammar**.

```

Block ::= block Identifier StateDeclaration* Transition* end
StateDeclaration ::= state State ;
Transition ::= transition Event : State -> State ;
Event ::= Identifier
State ::= Identifier
  
```

Formal Models Have a Semantics

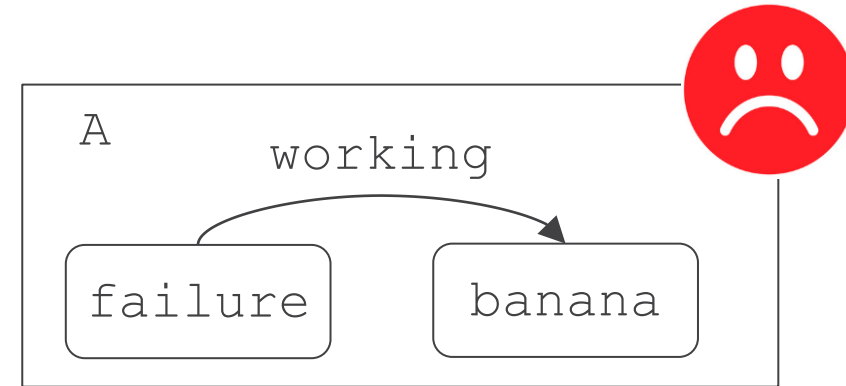
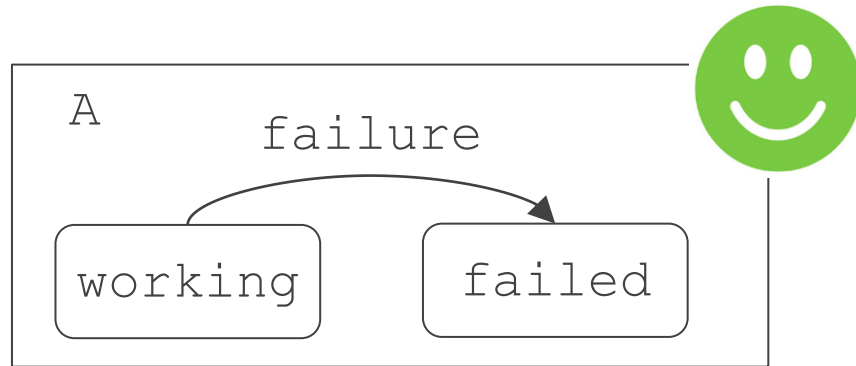


There should be an unambiguous way to interpret models into mathematical objects. This interpretation is the **semantics** of the model.

A formal semantics is the only way to justify computerized operations on models

Syntax and semantics are **domain independent**.

All Models Have a Pragmatics



Properties of models are interpreted into **properties of real systems**.
 This interpretation is called the **pragmatics** of models.

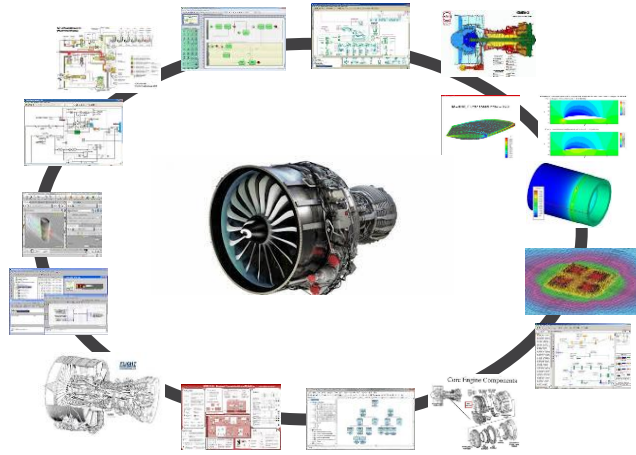
Facts about the pragmatics of models:

- It is at the very **core of the modeling process**.
- It is impossible to formalize as in requires a huge and **domain dependent** knowledge about systems.
- It is cultural and as such source of **ambiguities**.
- For these reasons, it should never be mixed up with the syntax and the semantics.

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Mathematical Frameworks



A model is always an **abstraction** of the system and is of interest because it is an abstraction.

The **properties of the system** to be studied determine the **mathematical framework** that should be used for the model.

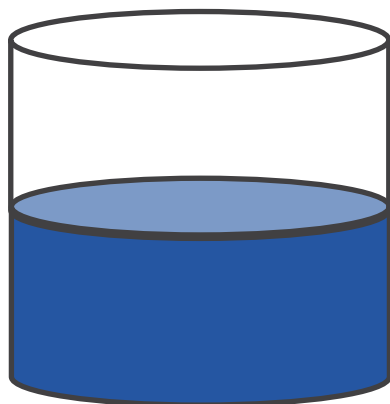
Experiments performed on the model have a **cost**. This cost is a key driver for the choice of the mathematical framework and the level of abstraction of the model.

The design of a model results always of a **tradeoff** between the **accuracy** of the description and the **cost** of experiments (calculations, simulations).

This is the reason why the **diversity** of models is **irreducible**.

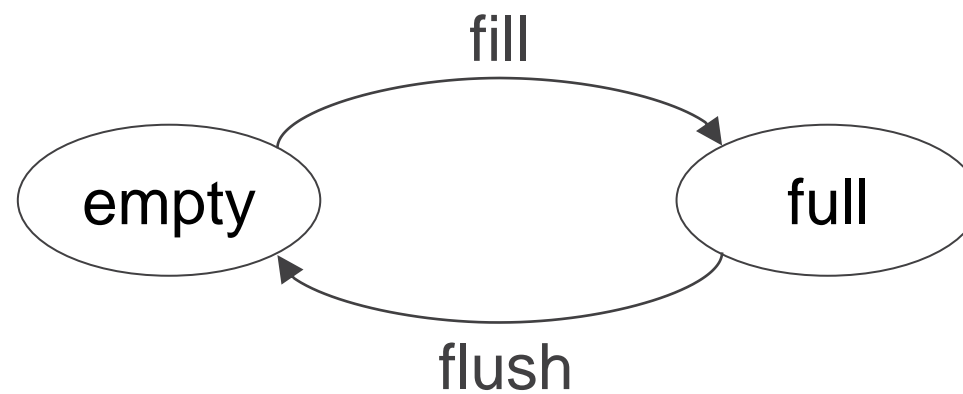
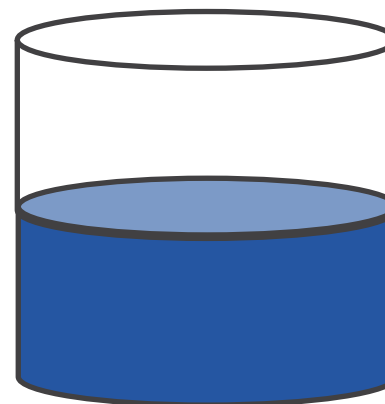
Mathematical Frameworks (bis)

Differential Equations



$$Q_{in} - Q_{out} = A \frac{dh}{dt}$$

Discrete Events



Mathematical Frameworks (ter)

Differential Equations

- At the core of physics
- Well mastered
- Powerful tools (Matlab/Simulink, Modelica)
- Very rich libraries of domain specific reusable modeling components
- Attempts to model systems (systems dynamics)
- Cost of simulations

Discrete Events

- More abstract vision (computer science)
- Better handling of non-deterministic and stochastic behaviors
- More efficient assessment tools

Classes of Event-Based Frameworks

The example of reliability engineering:

Combinatorial Formalisms

- Fault Trees
- Event Trees
- Reliability Block Diagrams
- Finite Degradation Structures

States Automata

- Markov chains
- Dynamic Fault Trees
- Stochastic Petri Nets
- AltaRica
- ...

Agent-Based Models

- Process algebras
- High level Petri nets
- ...

Expressive power

States

States + transitions

Deformable systems

Complexity of assessments

#P-hard but reasonable
 polynomial approximation

PSPACE-hard

Undecidable

Difficulty to design, to validate and to maintain models

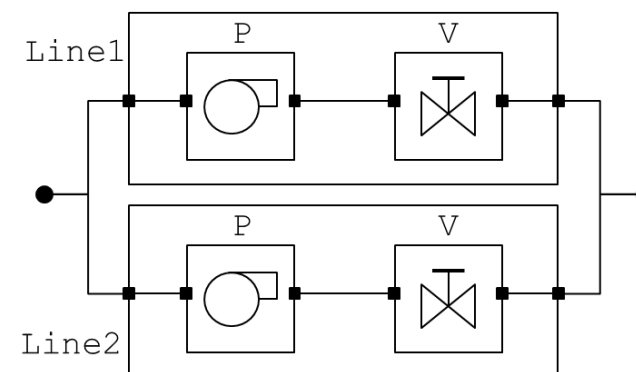
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Characteristics of Behavioral Models

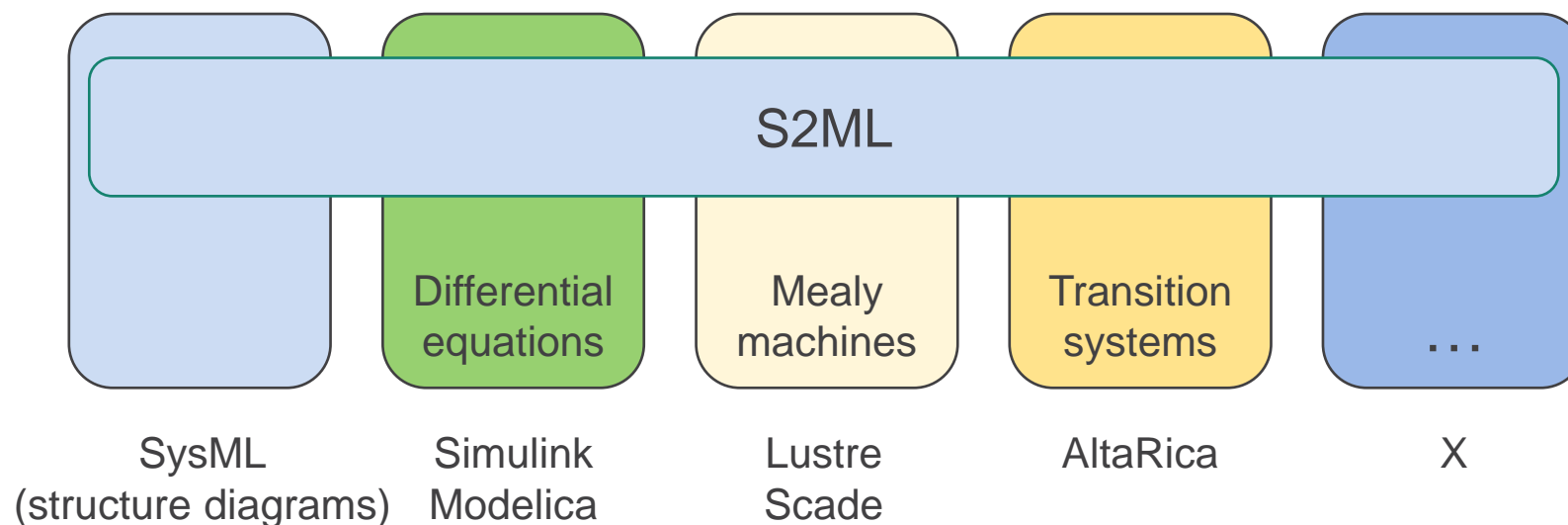
Behavior + Architecture = Model

- Any modeling language is the combination of a **mathematical framework** to describe the behavior and a **structuring paradigm** to organize the model.
- The choice of the **suitable mathematical framework** depends on which aspect of the system we want to study
- **Structuring paradigms** are to a very large extent **independent** of the chosen mathematical framework.



The S2ML+X Promise

S2ML (System Structure Modeling Language): a coherent and versatile set of **structuring constructs** for any behavioral modeling language.



- The **structure of models** reflects the **structure of the system**, even though to a **limited extent**.
- **Structuring** helps to design, to debug, to share, to maintain and to align heterogeneous models.

Models as Scripts

The **model "as designed"** is a script to build the **model "as assessed"**.

```
domain WF {WORKING, FAILED} WORKING<FAILED;

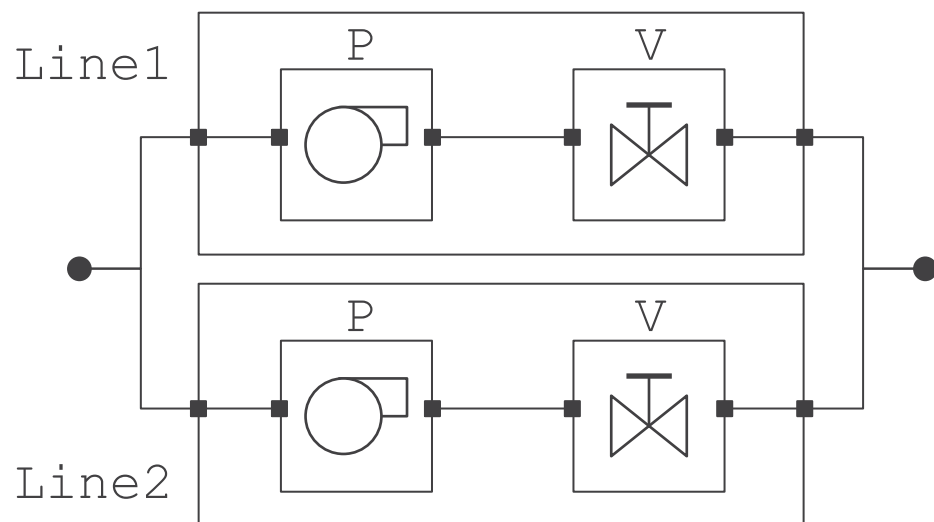
operator Series arg1 arg2 =
  return if state1==WORKING and state2==WORKING then WORKING else FAILED;

class Component
  WF state(init = WORKING);
  WF in, out(reset = WORKING)
  probability state FAILED = (exponentialDistribution lambda (missionTime));
  parameter Real lambda = 1.0e-3;
  assertion
    out := Series(in, state);
end
```

Complex models can be built using **libraries** of **reusable modeling components** and **modeling patterns**.

S2ML + Stochastic Boolean Equations

Enhancing classical **reliability models** (fault trees, reliability block diagrams) with the **expressive power of object-orientation** at **no algorithmic cost**

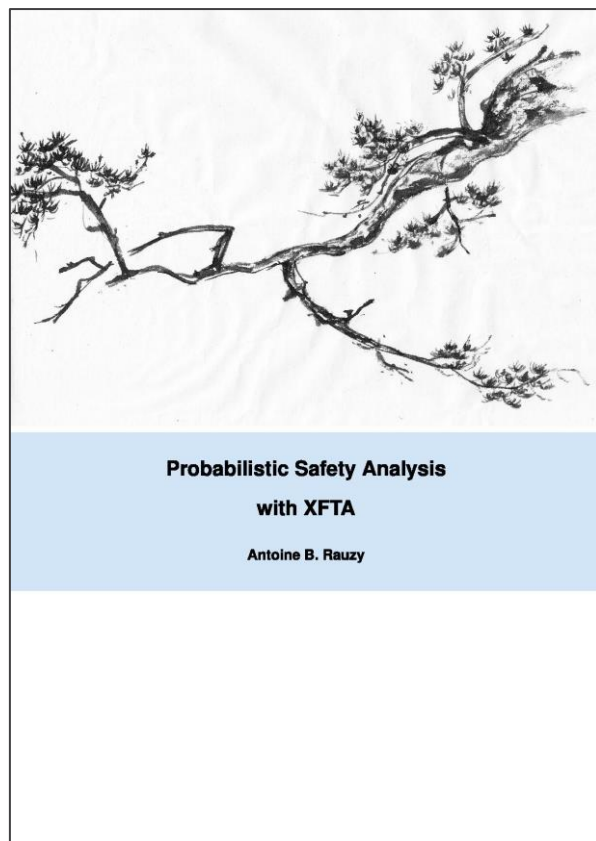


```
Line1.in := in;
Line1.P.in := Line1.in;
Line1.P.out := Line1.P.in and not Line1.P.failed;
...
```

```
class Pump
    extends RepairableUnit
    ...
end

block System
    block Line1
        Pump P;
        ...
    end
    clones Line1 as Line2;
    ...
end
```

XFTA 2 + XFTA Book



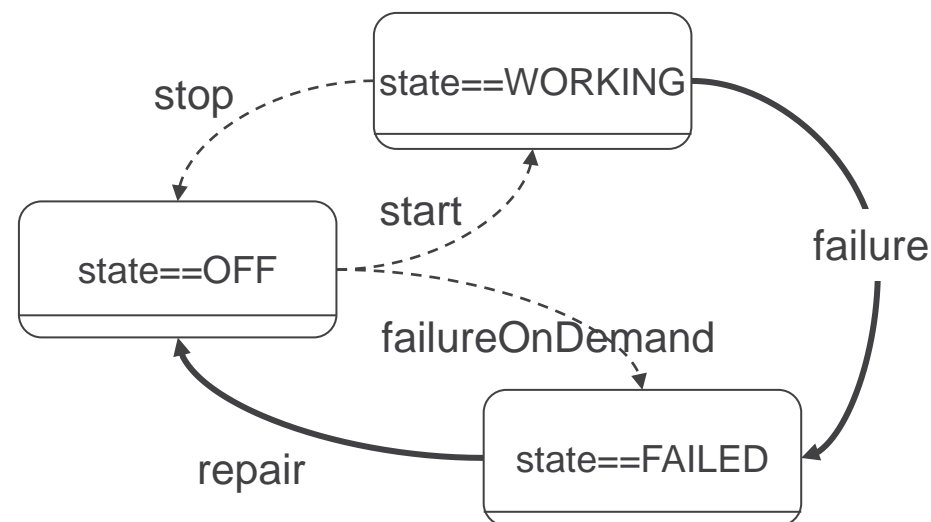
XFTA 2:

- Calculation engine for fault trees and related models.
- Input language: S2ML+SBE
- State of the art assessment algorithms: as of today, the most efficient calculation engine
- Calculation of all usual risk indicators:
 - Top event probability
 - Importance factors
 - Sensitivity analyses
 - Approximation of system reliability
 - Safety integrity levels
- Free of use.

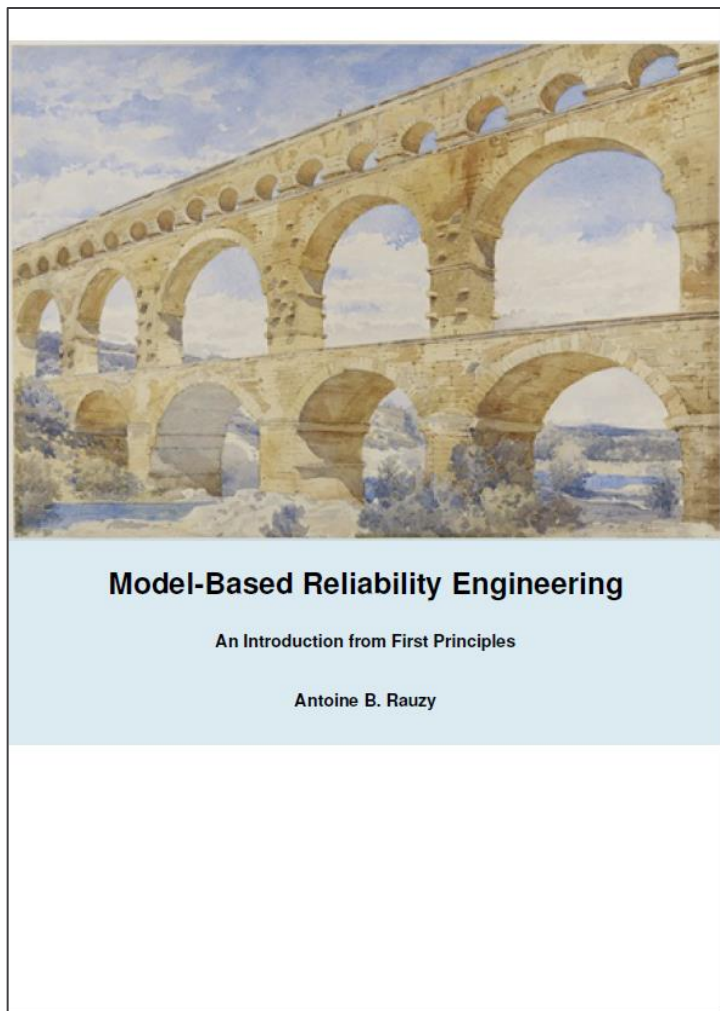
AltaRica 3.0 (S2ML + Guarded Transitions Systems)

Guarded Transitions Systems:

- Are a probabilistic Discrete Events System framework.
- Are a compositional formalism.
- Generalize existing other mathematical framework, e.g. Petri nets.
- Take the best advantage of existing assessment algorithms.



AltaRica Wizard + MBRE Book



Integrated Modeling Environment AltaRica Wizard:

- Supports AltaRica 3.0 and S2ML+SBE (XFTA)
- Efficient assessment tools (interactive simulator, compiler to SBE, compiler to Markov chains, generator of critical sequences, stochastic simulator).
- Free of use.

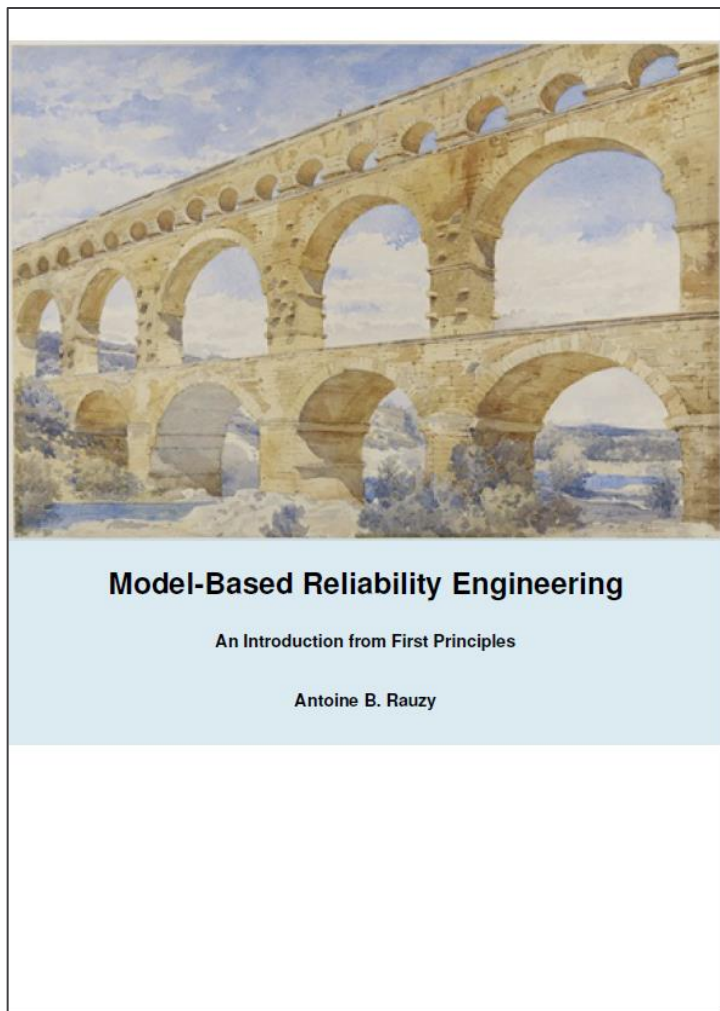
```

1 // A Block Diagram model for a simple High Pressure Protection System
2 // Using classes and inheritance
3
4 domain State (WORKING, FAILED)
5
6 class NonRepairableComponent
7   State _state (init=WORKING);
8   event Failure(delay=exponential(lambda));
9   parameter Real lambda = 1.0e-5;
10  transition
11    failure: _state==WORKING -> _state:=FAILED;
12 end
13
14 class NonRepairableInOutComponent extends NonRepairableComponent;
15   Boolean in(reset=false);
16   Boolean out(reset=false);
17   assertion
18     out := _state==WORKING and in;
19 end
20
21 class Sensor extends NonRepairableInOutComponent;
22 end
23
24 class SolenoidValve extends NonRepairableInOutComponent;
25 end
26
27 class ShutdownValve extends NonRepairableInOutComponent;
  
```

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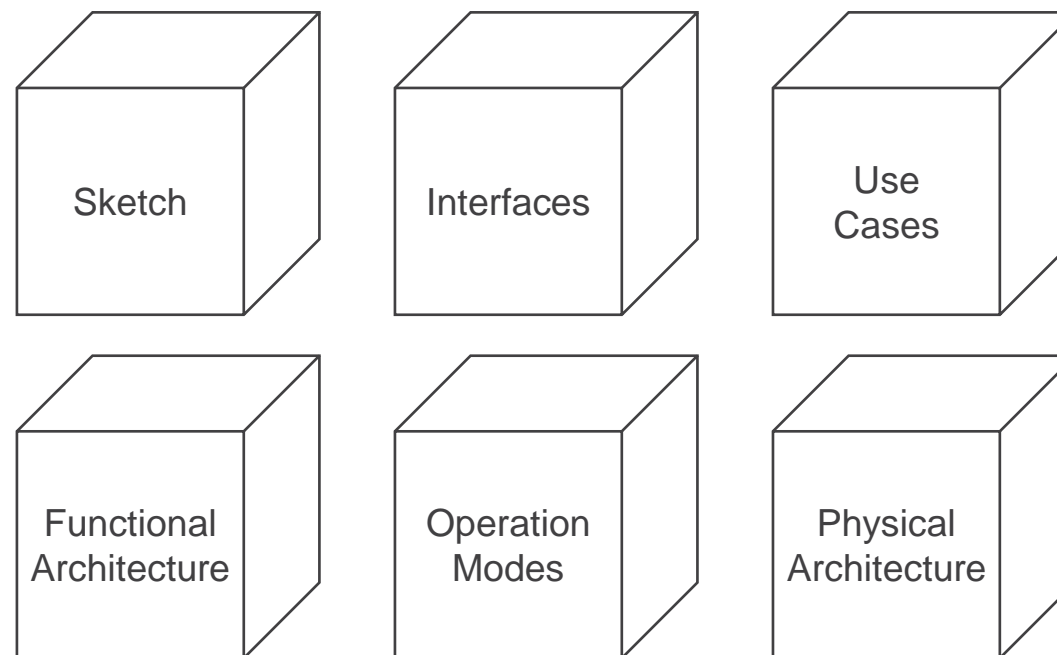
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Cube Architecture Framework



Architecture frameworks are sets of good practices and guidelines for creating, interpreting, analyzing and using descriptions of systems.

The **cube architecture framework** consists of 6 views:



Sigma (Σ)

A new S2ML+X language dedicated to the design of **systemic digital twins**

```

1  system World.Supplier
2    int rawMaterial(init = 0);
3    bool renewing(init = false);
4  end
5
6  activity World.Supplier.RenewRawMaterialStock
7    trigger:
8      return rawMaterial<=1000 and not renewing;
9    start:
10     renewing = true;
11    completion: {
12     renewing = false;
13     rawMaterial += 100;
14    }
15    duration:
16     return 30;
17  end

```

- Σ = S2ML + Activity Algebra
- Discrete events
- Reactive
- Deformable systems (systems of systems)
- Pragmatic proofs

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Conclusion

Huge benefits can be expected from a full-scale deployment of model-based systems engineering. However, this requires:

- To set up solid **scientific foundations**.
- To **bring to maturity** some **key technologies**.

The **biggest challenge** is to **train new generation of scientists and engineers**:

- With skills and competences in **discrete mathematics** and **computer science**,
- With skills and competences in **software engineering**,
- With skills and competences in **system thinking**,
- With skills and competences in **specific application domains**.



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